| Greek Letters |  | Common Usages |
| :---: | :---: | :---: |
| A $\alpha$ | Alpha | $\alpha$ : Constant in regression/statistics: $\mathrm{y}=\alpha+\beta \mathrm{x}+\varepsilon$; also type I error |
| B $\beta$ | Beta | $\beta$ : Coefficient in regression/statistics, often subscripted to indicate different coefficients: $y=$ $\alpha+\beta_{1} x_{1}+\beta_{2} X_{2}+\varepsilon$; also type II error; related, $1-\beta$ is called the "power" of a statistical test. |
| $\Gamma \gamma$ | Gamma | $\Gamma$ : A particular statistical distribution; also used to denote a game. |
| $\Delta \delta$ | Delta | $\Delta$ : Means "change" or "difference", as in the equation of a line's slope: $\frac{\Delta y}{\Delta x}=\frac{y_{1}-y_{2}}{x_{1}-x_{2}}$ <br> $\delta$ : Known in game theory as the "discount parameter" and is used for repeated games. |
| E $\varepsilon$ | Epsilon | $\varepsilon$ : "Error term" in regression/statistics; more generally used to denote an arbitrarily small, positive number. |
| $\epsilon$ | (Variant Epsilon) | This version of epsilon is used in set theory to mean "belongs to" or "is in the set of": $x \in \mathbf{X}$; similarly used to indicate the range of a parameter: $x \in[0,1]$. " $x \notin$ " means "the element $x$ does not belong to the empty set". |
| Z $\zeta$ | Zeta |  |
| $\mathrm{H} \mathrm{\eta}$ | Eta |  |
| $\Theta \theta$ | Theta | $\theta$ : The fixed probability of success parameter in a Binomial Distribution and related distributions. |
| $\vartheta$ | (Script Theta) |  |
| It | Iota |  |
| Кк | Карpa |  |
| $\Lambda \lambda$ | Lambda | $\lambda=n \theta$ : Parameter in the Poisson Distribution. |
| $\mathrm{M} \mu$ | Mu | $\mu$ : In statistics, the mean of a distribution. In game theory, often used as the probability of belief. |
| $\mathrm{N} V$ | Nu |  |
| $\Xi \xi$ | Xi |  |
| Oo | Omicron |  |
| $\Pi \pi$ | Pi | П: Product symbol, as in $\prod_{i=3}^{5} i=60$. <br> $\pi$ : Mathematical constant (3.14159...); also used in game theory to denote an actor's belief as a probability. |
| $\mathrm{P} \rho$ | Rho | $\rho$ : Correlation coefficient in some statistical analyses. |
| $\Sigma \sigma$ | Sigma | $\Sigma$ : Summation symbol, as in $\sum_{i=3}^{5} i=12$. <br> $\sigma$ : Standard Deviation of a distribution; also used to denote an actor's mixed strategy. $\sigma^{2}$ : Variance of a distribution. |
| $\checkmark$ | (Final Sigma) |  |
| $\mathrm{T} \tau$ | Tau |  |
| Yu | Upsilon |  |
| $\Phi \phi$ | Phi | $\Phi(z)$ : The cumulative density function (cdf) for the standard normal distribution. $\phi(z)$ : The probability density function (pdf) for the same. |
| $\varphi$ | (Script Phi) |  |
| $\mathrm{X} \chi$ | Chi | $\chi^{2}$ : A particular statistical distribution. |
| $\Psi \psi$ | Psi |  |
| $\Omega \omega$ | Omega | $\Omega:$ The "positive definite matrix" in regression/statistics. |
| $\varpi$ | (Variant Omega) |  |

## Mathematical Constants

| $\mathrm{e} \approx 2.718281828 \ldots$ | $\pi \approx 3.141592653 \ldots$ | $i=\sqrt{-1}$ (imaginary numbers) |
| :--- | :--- | :--- |


| Mathematical Symbols |  | Usage |
| :---: | :---: | :---: |
| ! | Factorial | $n!=\prod_{i=1}^{n} i ; \text { e.g., } 5!=5 \cdot 4 \cdot 3 \cdot 2 \cdot 1=120$ |
| $\wedge$ | "carrot" or "hat" | $3 \wedge 2=3^{2}=9$. Also used in statistics to denote estimates: $\hat{\sigma}$ |
| $\overline{\mathbf{X}}$ | x "bar" | Sample mean of $\mathbf{X}=(\Sigma x) / n$, where $n$ is the number of observations. |
| $\forall$ | All | $\forall x$; for all $x$, something is true. |
| $\exists$ | Exists | $\exists x=1$; there exists some $x$ equal to 1 . |
| $\rightarrow$ | Implies | $p \rightarrow q$; if $p$ is true (or occurs), then $q$ is true (or will occur). |
| $\therefore$ | Therefore | Indicating a logical result: $p \rightarrow q$ and $q \rightarrow r, \therefore p \rightarrow r$. |
| 1 | Given, Conditional | $\mathrm{P}(\mathbf{E} \mid \mathbf{F})$; The probability of $\mathbf{E}$ given (or within the set of) $\mathbf{F}$. |
| \| | Absolute Value | $\|-x\|=x$ |
| $\sim$ | Not | $\sim \mathrm{C}$; not to cooperate. (Also used in geometry to mean "similar".) |
| $\leq$ | Less than or equal to |  |
| $\geq$ | Greater than or equal to |  |
| $\infty$ | Infinity |  |
| $\pm$ | Plus or minus |  |
| $\propto$ | Proportional to | $x \propto 1 / f$ |
| $\partial$ | Derivative | Calculus notation; $\frac{\partial}{\partial x}(y=m x+b)=m$ |
| \# | Not equal to |  |
| 三 | Identically equal to | $x \equiv x$; sometimes a way proving something; also a way of denoting a definition. |
| $\approx$ | Approximately equal to | $\pi \approx 3.14$ |
| $\mathfrak{R}, \mathbf{R}, \text { or }$ | Set of Real Numbers |  |
| $\varnothing$ | Empty Set | $\mathbf{X}=\varnothing$; The set $\mathbf{X}$ is empty. $\mathbf{X} \neq \varnothing$; The set $\mathbf{X}$ is not empty. |
| $\bigcirc$ | Conjunction; And | $\{1,2,3,4\} \cap\{4,5,6,7\}=\{4\}$ |
| $\cup$ | Union; Or | $\{1,2,3,4\} \cup\{4,5,6,7\}=\{1,2,3,4,5,6,7\}$ |
| $\checkmark$ | Square root | $\sqrt{2} \approx 1.414 ; \sqrt{4}=2$ |
| $\mathrm{P}(\cdot)$ | Probability of | $\mathrm{P}(\mathrm{HH})=1 / 2 \cdot 1 / 2=1 / 4$; the probability of landing two heads in successive coin flips; sometimes $\operatorname{Pr}(\cdot)$. |
| $L$ | Likelihood | Used in Maximum Likelihood Estimation in statistics. |
| $\mathrm{L}(\cdot)$ | Lottery (in game theory) | $\mathrm{L}(B, W ; p)$ is a lottery between winning one's best outcome, $B$, with probability $p$ and "winning" one's worst outcome, $W$, with probability $1-p$. |
| $\mathrm{E} \cdot$ ) | Expectation of | $\mathrm{E}(\mathrm{X})=\Sigma x \cdot \mathrm{P}(x)$; also as expected utility: $\mathrm{EU}(\mathrm{L}(1,0 ; 1 / 4))=1 \cdot 1 / 4+0 \cdot 3 / 4=1 / 4$. |
| $\ln$ or LN | Natural log | $(\ln (x)=\mathrm{b}) \equiv\left(\mathrm{e}^{\mathrm{b}}=\mathrm{x}\right)$, where e is the mathematical constant. |
| lim | Limit | $\lim _{x \rightarrow \infty} \frac{1}{x}=0$; The limit of $1 / x$ as $x$ goes to (or approaches) infinity equals zero. |
| $\int$ | Integral | Calculus notation; $\int x d x=\frac{1}{2} x^{2}$ and $\int_{a}^{b} \frac{1}{a+b} d x=\frac{b-a}{a+b}$ |
|  |  |  |
| J | Jacobian | J: a particular matrix; J: Determinant of a Jacobian matrix. |

## Rules of Logic

| p |  | Addition |
| :---: | :---: | :---: |
| $\therefore \mathrm{p} \cup \mathrm{q}$ |  |  |
| p |  | Conjunction |
| q |  |  |
| $\therefore \mathrm{p} \cap \mathrm{q}$ |  |  |
| $\mathrm{p} \cap \mathrm{q}$ |  | Simplification |
| $\therefore \mathrm{p}$ |  |  |
| $\therefore \mathrm{q}$ |  |  |
| $\underset{\sim}{p} \cup \underset{\sim}{q}$ |  | Elimination |
| $\therefore \mathrm{q}$ |  |  |
| $\sim(\sim p)$ |  | Double Negation |
| $\therefore \mathrm{p}$ |  |  |
| $\sim(\mathrm{p} \cup \mathrm{q})$ | $\sim(\mathrm{p} \cap \mathrm{q})$ | De Morgan’s Rule |
| $\therefore \sim \mathrm{p} \cap \sim \mathrm{q}$ | $\therefore \sim p \cup \sim q$ |  |
| $\mathrm{p} \rightarrow \mathrm{q}$ | $\mathrm{p} \rightarrow \mathrm{q}$ | Implication |
| $\therefore \sim \mathrm{p} \cup \mathrm{q}$ | $\therefore \sim(\mathrm{p} \cap \sim \mathrm{q})$ |  |
| $\begin{aligned} & \mathrm{p} \rightarrow \mathrm{q} \\ & \mathrm{p} \end{aligned}$ |  | Modus Ponens |
| $\therefore \mathrm{q}$ |  |  |
| $\mathrm{p} \rightarrow \mathrm{q}$ |  | Modus Tollens |
| $\sim \mathrm{q}$ |  |  |
| $\therefore \sim p$ |  |  |
| $\mathrm{p} \rightarrow \mathrm{q}$ | $\sim \mathrm{q} \rightarrow \sim \mathrm{p}$ | Contrapositive or Transposition |
| $\therefore \sim \mathrm{q} \rightarrow \sim \mathrm{p}$ | $\therefore \mathrm{p} \rightarrow \mathrm{q}$ |  |
| $\mathrm{p} \rightarrow \mathrm{q}$ |  | Chain Rule |
| $\mathrm{q} \rightarrow \mathrm{r}$ |  |  |
| $\therefore \mathrm{p} \rightarrow \mathrm{r}$ |  |  |
| $\mathrm{p} \leftrightarrow \mathrm{q}$ | $\mathrm{p} \rightarrow \mathrm{q}$ | Biconditional |
| $\therefore \mathrm{p} \rightarrow \mathrm{q}$ | $\mathrm{q} \rightarrow \mathrm{p}$ |  |
| $\therefore \mathrm{q} \rightarrow \mathrm{p}$ | $\therefore \mathrm{p} \leftrightarrow \mathrm{q}$ |  |

