

# Preliminary results from an agent-based adaptation of friendship games

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# Outline

- 1 Friendship Games
- 2 Generating a Random Network

## Lamberson (2011)

- Based on Galeotti et al. (2010) *Network Games*: agent payoff depends on own actions and the actions of neighbors in a social network.
- **Strategic complement** - network externality (widely adopted software)
- **Strategic substitute** - privately provided public good (streetlight, security, power tools)

## Strategic complements

Suppose there are two strategies,  $x$  and  $y$ . If an agent has  $k$  friends, then, at any given instance, there are  $k_x$  of them playing strategy  $x$ , and  $k_y$  of them playing strategy  $y$ . For the strategic complements models, the payoff for playing strategy  $x$  is

$$\pi_x(k_x) = f(k_x) - c_x$$

and the payoff for playing strategy  $y$  is

$$\pi_y(k_x) = f(1 - k_x) - c_y$$

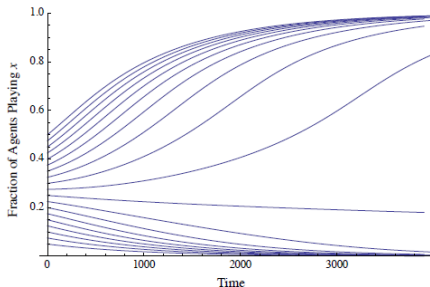
where  $f$  is a non-decreasing function and  $c_x$  and  $c_y$  are the costs of play  $x$  and  $y$ , respectively.



## Lamberson strategic complements

Play strategy  $x$  if four or more neighbors (in a random network of mean degree 10) are playing  $x$ .

$$\pi_x^{\text{complement}} = \begin{cases} 1 & k_x \geq 4 \\ 0 & \text{otherwise} \end{cases}$$



## Strategic substitutes

For the strategic substitutes models, the payoff for playing strategy  $x$  is

$$\pi_x(k_x) = 1 - c_x$$

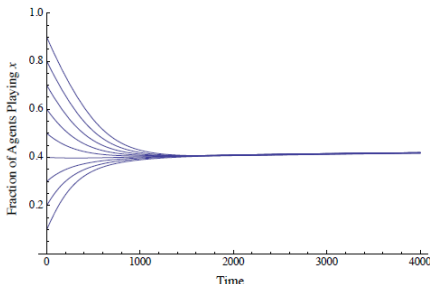
where  $0 < c_x < 1$  and the payoff for playing strategy  $y$  is

$$\pi_y(k_x) = \begin{cases} 1 & k_x \geq 1 \\ 0 & \text{otherwise} \end{cases}$$

## Lamberson strategic substitutes

Play strategy  $x$  if four or fewer neighbors (in a random network of mean degree 10) are playing  $x$ .

$$\pi_x^{substitute} = \begin{cases} 1 & k_x \leq 4 \\ 0 & \text{otherwise} \end{cases}$$



# Generating a Random Network

- NetLogo doesn't have a random graph capability per se
- NetLogo doesn't allow loops over loops of turtles
- Completely random selection of all possible pairs is time consuming
- For a Gilbert random graph  $G(n,p)$ , each edge in the graph has probability  $p$

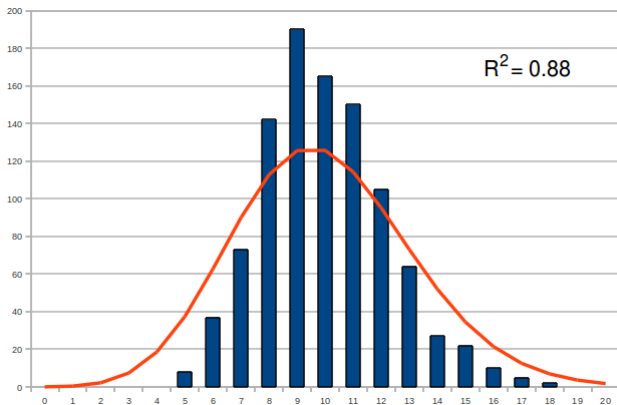


## Random Network (first attempt)

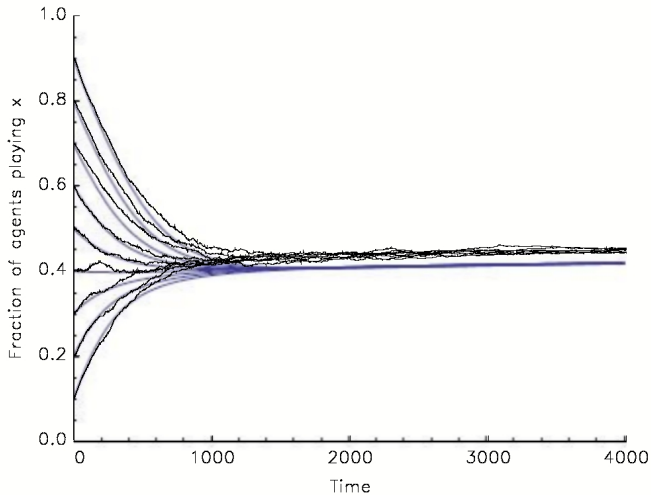
- The mean number of degree (links per turtle) is  $pn$
- Approach: for each turtle, try to create links to  $pn$  other random turtles

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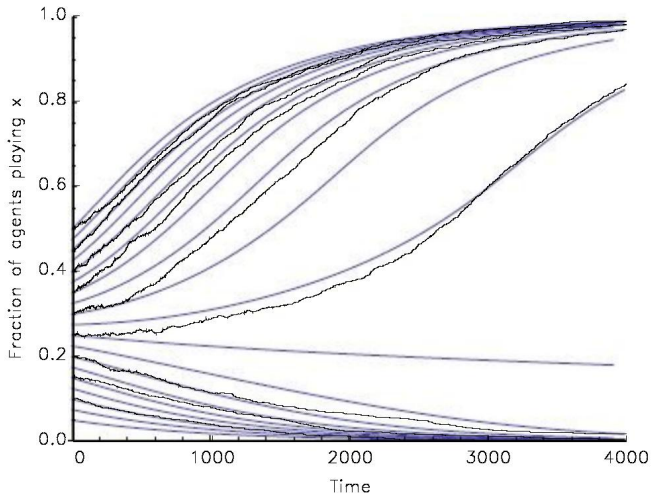
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# Friendship ABM - substitutes



# Friendship ABM - complements

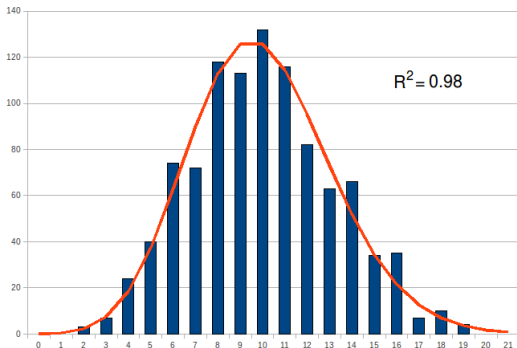


## Random Network (second attempt)

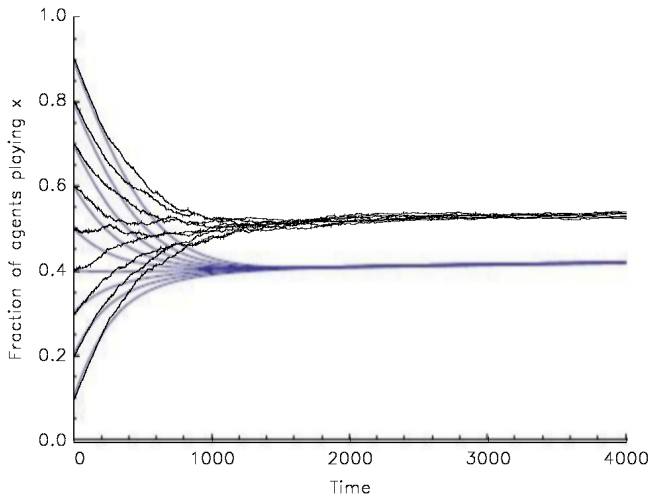
- A random graph with  $n$  nodes has  $\frac{n^2}{2}$  unique (undirected) edges, and for edge probability  $p$ , the total number of edges (links) is  $n_l = \frac{pn^2}{2}$
- Approach: link random pairs of turtles until there are  $n_l$  links

## Random Network (second attempt)

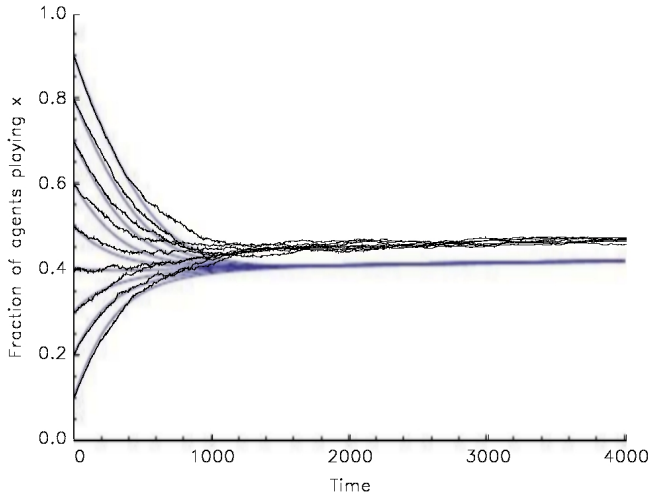
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- Approach: link random pairs of turtles until there are  $n_l$  links



## Friendship ABM (2) - substitutes

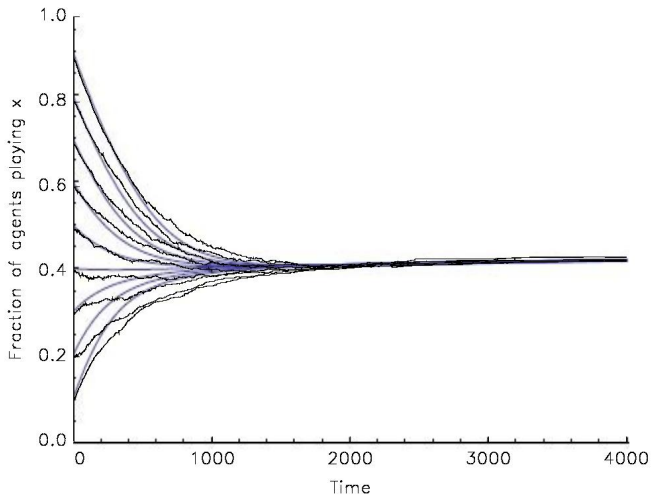


# Endpoint error?

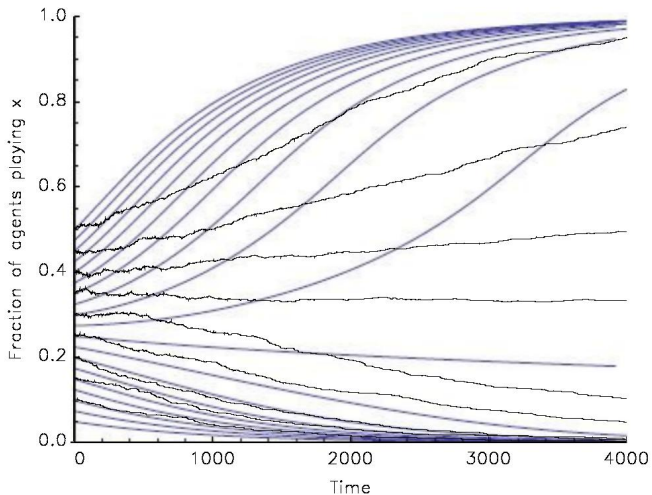




## 2-Regular Network - substitutes



## 2-Regular Network - complements



# Summary

- ABM equivalent of a network game is sensitive to the network topology
- Gilbert random graph  $G(1000,0.01)$  is close but not as close as expected
- 2-regular graph is very close on substitutes, very far on complements
- Outlook
  - Results from 10-regular graph will be instructive
  - Once the network topology is worked out, shocks, preference switching, innovation, extensive-form games...