

Math 180 - Homework #1

Write the ANSWERS ONLY on this page. Do your calculations/work elsewhere, then NEATLY transfer your answers to this page.

Differentiate the following (2pts. each):

ANSWER

1. $y = x^7 + x^3$

$$y' = 7x^6 + 3x^2$$

2. $y = 5x^8$

$$y' = 40x^7$$

3. $y = 6\sqrt{x}$

$$y' = 3x^{-1/2} = \frac{3}{\sqrt{x}}$$

4. $y = x^7 + 3x^5 + 1$

$$y' = 7x^6 + 15x^4$$

5. $y = \frac{3}{x}$

$$y' = -3x^{-2} = -\frac{3}{x^2}$$

6. $y = x^4 - \frac{4}{x}$

$$y' = 4x^3 + 4x^{-2} = 4x^3 + \frac{4}{x^2}$$

7. $y = \frac{3}{4}x^{\frac{4}{3}} + \frac{4}{3}x^{\frac{3}{4}}$

$$y' = x^{\frac{1}{3}} + x^{-\frac{1}{4}}$$

8. $y = \frac{1}{\sqrt[4]{x}}$

$$y' = -\frac{1}{4}x^{-5/4} = -\frac{1}{4x^{5/4}}$$

9. $f(x) = 5$

$$f'(x) = 0$$

10. $f(x) = \frac{5x}{2} - \frac{2}{5x}$

$$f'(x) = \frac{5}{2} + \frac{2}{5}x^{-2}$$

11. $f(t) = t^{10} - 10t^9$

$$f'(t) = 10t^9 - 90t^8$$

12. $g(t) = 3\sqrt{t} - \frac{3}{\sqrt{t}}$

$$g'(t) = \frac{3}{2}t^{-1/2} + \frac{3}{2}t^{-3/2}$$

13. $h(t) = 3\sqrt{2}$

$$h'(t) = 0$$

14. $g(P) = 4P^{0.7}$ (Decimals in answer OK for this problem only)

$$g'(P) = 2.8P^{-0.3}$$

15. $h(x) = \frac{3}{2}x^{\frac{3}{2}} - 6x^{\frac{2}{3}}$

$$h'(x) = \frac{9}{4}x^{1/2} - 4x^{-1/3}$$

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Differentiate the following (2pts. each):

ANSWER

$$16. \frac{d}{dx}(x^4 - 2x^2)$$

$$(4x^3 - 4x)dx$$

$$17. \frac{d}{dt}\left(t^{\frac{5}{2}} + 2t^{\frac{3}{2}} - t^{\frac{1}{2}}\right)$$

$$\left(\frac{5}{2}t^{\frac{3}{2}} + 3t^{\frac{1}{2}} - \frac{1}{2}t^{-\frac{1}{2}}\right)dt$$

$$18. \frac{d}{dn}(n^{-5})$$

$$(-5n^{-6})dn$$

$$19. \frac{d}{dt}(2\sqrt{t})$$

$$\left(t^{-\frac{1}{2}}\right)dt = \left(\frac{dt}{\sqrt{t}}\right)$$

$$20. \frac{d}{dx}\left(\frac{x^3 - 4x^2 + 3}{x}\right) \quad (\text{Hint: Reduce/Simplify fraction to 3 individual terms each with a single } \pm \text{ exponent, then differentiate each term separately})$$

$$(2x - 4 - 3x^{-2})dx = \left(2x - 4 - \frac{3}{x^2}\right)dx$$

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Integrate the following (2pts. each):

ANSWER

$$21. \int x(1 + x^3)dx \quad (\text{Hint: Distribute FIRST, then integrate})$$

$$\frac{1}{2}x^2 + \frac{1}{5}x^5 + C$$

$$22. \int x^{\frac{1}{3}}(2 - x)^2 dx \quad (\text{Hint: FOIL, then distribute, THEN integrate})$$

$$3x^{\frac{4}{3}} - \frac{12}{7}x^{\frac{7}{3}} + \frac{3}{10}x^{\frac{10}{3}} + C$$

$$23. \int \frac{x^6 + 2x^2 - 1}{x^2} dx \quad (\text{Hint: Reduce/Simplify fraction to 3 individual terms each with a single } \pm \text{ exponent, then integrate each term separately})$$

$$\frac{1}{5}x^5 + 2x + x^{-1} + C = \frac{1}{5}x^5 + 2x + \frac{1}{x} + C$$

$$24. \int \left(x^{-3} + \sqrt{x} - 3x^{\frac{1}{4}} + x^2\right) dx$$

$$-\frac{1}{2}x^{-2} + \frac{2}{3}x^{\frac{3}{2}} - \frac{12}{5}x^{\frac{5}{4}} + \frac{1}{3}x^3 + C$$

$$25. \int_2^3 \left(1 - \frac{1}{2}x\right) dx \quad \text{ANSWER AS A FRACTION. NO DECIMALS!}$$

$$-\frac{1}{4}$$

$$26. \int_{-10}^{-5} 6dx$$

$$30$$

$$27. \int_{-3}^0 (x^2 - 4x + 7)dx$$

$$48$$

$$28. \int_4^9 (2x\sqrt{x}) dx \quad (\text{Hint: Simplify to a SINGLE fractional exponent, then integrate})$$

ANSWER AS A FRACTION. NO DECIMALS!

$$\frac{844}{5} = 168\frac{4}{5} = 168.8$$

$$29. \int_1^3 \frac{1}{x^2} dx \quad \text{ANSWER AS A FRACTION. NO DECIMALS!}$$

$$\frac{2}{3}$$

$$30. \int_{-1}^0 \frac{x^2 - x + 3}{\sqrt[3]{x}} dx \quad (\text{Hint: Reduce/Simplify fraction to 3 individual terms each with a single } \pm \text{ exponent, then integrate each term separately})$$

ANSWER AS A FRACTION. NO DECIMALS!

$$-\frac{219}{40} = -5\frac{19}{40} = -5.475$$