

HW # 6

2.11. $N_D = 10^{18} - 10^{16} = 9.9 \times 10^{17} \text{ cm}^{-3}$

$$n_0 p_0 = n_i^2 \Rightarrow 9.9 \times 10^{17} \times p_0 = (1.062 \times 10^{10})^2$$

$$p_0 = 114 \text{ cm}^{-3}$$

2.13.

$$p_0 = 4 \times 10^6 \text{ cm}^{-3}$$

$$N_D - N_A = 4.99 \times 10^{18}$$

$$p_0 = \frac{n_i^2}{N_D - N_A} \Rightarrow n_i = \sqrt{p_0 (N_D - N_A)} = 4.468 \times 10^{12} \text{ cm}^{-3}$$

$$n_i = BT^{3/2} e^{\frac{-E_g}{2kT}}$$

$$B = 5.23 \times 10^{15}$$

$$E_g = 1.12 \text{ eV}$$

$$k = 85.17 \frac{\text{MeV}}{\text{K}}$$

$$\Rightarrow 4.468 \times 10^{12} = 5.23 \times 10^{15} \cdot T^{3/2} \exp\left(-\frac{1.12}{2kT}\right)$$

$$T = 404.43 \text{ K}$$

2.15

a) $E = \frac{V}{d} = \frac{1 \text{ V}}{20 \times 10^{-4} \text{ cm}} = 500 \frac{\text{V}}{\text{cm}}$

b) $n_0 p_0 = n_i^2$

$$n_i = BT^{3/2} e^{\left(-\frac{E_g}{2kT}\right)}$$

$$n_i = 5.23 \times 10^{15} \times (280)^{3/2} \cdot e^{\left(-\frac{1.12}{2 \times 8617 \times 280}\right)} = 2.04 \times 10^9 \text{ cm}^{-3}$$

$$n_o = \frac{n_i^2}{p_o} = \frac{(2.04 \times 10^9)^2}{10^{18}} = 4.16 \text{ cm}^{-3}$$

$$\begin{aligned} \text{c) } J &= \mu_n q E n_o + \mu_p q E p_o \\ &= 1500 \times 1.6 \times 10^{-19} \times 500 \times 4.16 + 500 \times 1.6 \times 10^{-19} \times 500 \times 10^{18} \\ J &= 40050 \text{ A/cm}^2 \end{aligned}$$

$$\text{d) } J = 40050 \frac{\text{A}}{\text{cm}^2} \times \left(10^{-4} \frac{\text{cm}}{\mu}\right)^2 = 400.5 \frac{\mu\text{A}}{\text{cm}^2}$$

2.20.

$$J_{n,diff} = q D_n \frac{dn_o}{dx} \quad , \quad J_{p,diff} = q D_p \frac{dp_o}{dx}$$

$$J = q D_n \frac{dn_o}{dx} + q D_p \frac{dp_o}{dx}$$

$$\frac{dn_o}{dx} = 3 \frac{dp_o}{dx}$$

$$J = q D_n \cdot 3 \frac{dp_o}{dx} + q D_p \frac{dp_o}{dx} = q D_n \frac{dn_o}{dx} + q D_p \frac{1}{3} \frac{dn_o}{dx}$$

$$15 \frac{\text{mA}}{\text{cm}^2} = 1.6 \times 10^{-19} \times 35 \times 3 \frac{dp_o}{dx} + 1.6 \times 10^{-19} \times 12 \times \frac{dp_o}{dx}$$

$$\frac{dp_o}{dx} = 8.013 \times 10^{14} \text{ cm}^{-1}$$

$$15 \frac{\text{mA}}{\text{cm}^2} = 1.6 \times 10^{-19} \times 35 \times \frac{dn_0}{dx} + 1.6 \times 10^{-19} \times 12 \times \frac{1}{3} \frac{dn_0}{dx}$$

$$\frac{dn_0}{dx} = 2.404 \times 10^{15} \text{ cm}^{-1}$$

2.24

$$a) V_{bi} = \frac{kT}{q} \ln \left(\frac{N_A N_D}{n_i^2} \right) \quad T = 300 \text{ K}$$

$$V_{bi} = \frac{1.38066 \times 10^{-23} \times 300}{1.6 \times 10^{-19}} \ln \left(\frac{10^{16} \times 10^{18}}{(1.062 \times 10^{10})^2} \right) = 0.831 \text{ mV}$$

$$b) T = 400 \text{ K}$$

$$n_i = BT^{3/2} e^{-\frac{E_g}{2kT}} = 5.23 \times 10^{15} \times 400^{3/2} \exp\left(-\frac{1.12}{2k \times 400}\right)$$

$$n_i = 3.678 \times 10^{12}$$

$$V_{bi} = \frac{kT}{q} \ln \left(\frac{N_A N_D}{n_i^2} \right)$$

$$V_{bi} = \frac{1.38066 \times 10^{-23} \times 400}{1.6 \times 10^{-19}} \ln \left(\frac{10^{16} \times 10^{18}}{(3.678 \times 10^{12})^2} \right) = 0.705 \text{ V}$$

2.28.

$$I_0 = I_S \left(e^{\frac{qV_0}{kT}} - 1 \right)$$

2.28

$$I_D = 10 \mu\text{A} \left(e^{\frac{1.6 \times 10^{-19} \times 0.625}{1.38066 \times 10^{-23}}} - 1 \right) = 275 \text{ mA}$$

2.30

$$I_D = I_S \left(e^{\frac{V_D}{V_{th}}} - 1 \right) \approx I_S \cdot e^{\frac{V_D}{V_{th}}}$$

$$\frac{I_{D1}}{I_{D2}} = e^{\frac{V_{D1} - V_{D2}}{V_{th}}} = e^{\frac{\Delta V}{V_{th}}}$$

$$\Delta V = V_{th} \cdot \ln\left(\frac{I_{D1}}{I_{D2}}\right) = 25.9 \text{ mV} \times \ln(100) = 0.119 \text{ V}$$