

$$\begin{aligned}
& K'_n \left(\frac{W}{L}\right)_n \left[(V_m - V_{tn}) V_{DSATn} - \frac{V_{DSATn}^2}{2} \right] (1 + \lambda_n V_{DS}) \\
&= K'_p \left(\frac{W}{L}\right)_p \left[(V_{DD} - V_m - V_{tp}) V_{DSATp} - \frac{V_{DSATp}^2}{2} \right] (1 + \lambda_p (V_{DD} - V_m)) \\
&\Rightarrow 115 \frac{\text{MA}}{\text{V}^2} \times 1.5 \times \left[(1.25 - 0.43) \times 0.63 - \frac{0.63^2}{2} \right] (1 + 0.06 \times 1.25) \\
&= 30 \frac{\text{MA}}{\text{V}^2} \times \left(\frac{W}{L}\right)_p \left[(2.5 - 1.25 - 0.4) \times 0.8 - \frac{0.8^2}{2} \right] (1 + 0.1 \times (2.5 - 1.25)) \\
&\Rightarrow \left(\frac{W}{L}\right)_p = 5.1
\end{aligned}$$

2. Estimate all static parameters of the inverter in problem 1, including V_{OL} , V_{OH} , V_M , V_{IL} , V_{IH} , NML , and NMH .

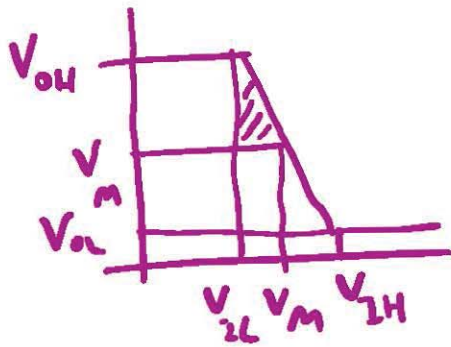
$$V_{OL} = 0\text{V}, \quad V_{OH} = 2.5\text{V}, \quad V_M = 1.25\text{V}$$

$$g = \frac{1}{I_D(V_M)} \frac{K'_n \left(\frac{W}{L}\right)_n V_{DSATn} + K'_p \left(\frac{W}{L}\right)_p V_{DSATp}}{\lambda_n + \lambda_p}$$

$$\begin{aligned}
\frac{I_D(V_M)}{1} &= 115 \frac{\text{MA}}{\text{V}^2} \times 1.5 \times \left[(1.25 - 0.43) \times 0.63 - \frac{0.63^2}{2} \right] (1 + 0.06 \times 1.25) \\
&= 59 \text{MA}
\end{aligned}$$

$$\Rightarrow g = \frac{115 \frac{\text{MA}}{\text{V}^2} \times 1.5 \times 0.63 + 30 \frac{\text{MA}}{\text{V}^2} \times 5.1 \times 0.8}{59 \text{MA} \times (0.06 + 0.1)}$$

$$\Rightarrow |g| = 24.48$$



$$|g| = \frac{V_{OH} - V_M}{V_M - V_{IL}}$$

$$\Rightarrow 24.48 = \frac{2.5 - 1.25}{1.25 - V_{IL}}$$

$$\Rightarrow \underline{V_{IL} = 1.199 \text{ V}}$$

$$|g| = \frac{V_M - V_{OL}}{V_{IH} - V_M} \Rightarrow 24.48 = \frac{1.25 - 0}{V_{IH} - 1.25}$$

$$\Rightarrow \underline{V_{IH} = 1.301 \text{ V}}$$

$$NMH = V_{OH} - V_{IH} = 2.5 - 1.301 = \underline{1.199 \text{ V}}$$

$$NML = V_{IL} - V_{OL} = 1.199 - 0 = \underline{1.199 \text{ V}}$$