

$$[\gamma^a, \gamma^b] \partial_a \partial_b = 0$$

$$\left(\begin{array}{cc} a=1 & b=2 \\ a=2 & b=1 \end{array} \right.$$

$$\rightarrow (\gamma^1 \gamma^2 - \gamma^2 \gamma^1) \partial_1 \partial_2$$

$$+ (\gamma^2 \gamma^1 - \gamma^1 \gamma^2) \partial_2 \partial_1 = 0$$

$$\sum_{a,b=1}^3 [\gamma^a, \gamma^b] \partial_a \partial_b = 0$$

$$\gamma^a$$

$$4 \times 4$$

$$\{\gamma^a, \gamma^b\} = \gamma^a \gamma^b + \gamma^b \gamma^a$$

$$\gamma^0 \quad \begin{pmatrix} 1 & 0 & 0 & 0 \\ 0 & -1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & -1 \end{pmatrix}$$

$$= 2 \eta^{\mu\nu} = 2 \begin{pmatrix} 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 0 \end{pmatrix}$$

$$\eta' = -\eta.$$

$$\{x^i, x^k\} = 2 g^{ik}$$

$$i, k = 0, 1, 2, 3$$

$$x^i = C^i_a x^a$$

$$\{x^i, x^k\} = C^i_a C^k_b \{x^a, x^b\}$$

$$= 2 C^i_a C^k_b \eta^{ab}$$

$$= 2 g^{ik}$$

$$g_{ik} = C^a_i \eta_{ab} C^b_k$$

$$ds^2 = g_{ik} dx^i dx^k$$

$$\int_a^b p f u_k dx = \int_a^b p \left(\sum c_j u_j \right) u_k dx$$

$$= c_j \delta_{jk} = c_k$$

$$f(x) = \sum_{k=1}^{\infty} a_k \underbrace{u_k(x)}_{\text{e.f.as.}}$$

$$a_k = \int_a^b dx \, p(x) u_k(x) f(x)$$

$$\begin{aligned} f(x) &= \sum_{k=1}^{\infty} u_k(x) \int_a^b dy \, p(y) u_k(y) f(y) \\ &= \int_a^b dy \, f(y) \left[\sum_{k=1}^{\infty} p(y) u_k(x) u_k(y) \right] \\ &= \int_a^b dy \, f(y) \delta(x-y) \end{aligned}$$

∞

$$\begin{aligned}\delta(x-y) &= \rho(y) \sum_{k=1}^{\infty} u_k(x) u_k(y) \\ &= \rho(x) \sum_{k=1}^{\infty} u_k(x) u_k(y)\end{aligned}$$

$$\delta(x) = \rho(x) \sum_{k=1}^{\infty} u_k(x) u_k(0)$$

$$\delta(x-y) = \rho(x) \sum_{k=1}^{\infty} u_k(x) u_k(y)$$

$$\mathcal{L} G(x-y) = \delta(x-y)$$

$$G(x-y) = \sum_{k=1}^{\infty} c_k u_k(x) u_k(y)$$

$$\begin{aligned}\mathcal{L}_x G(x-y) &= \sum_k \mathcal{L}_x u_k(x) u_k(y) c_k \\ &= \sum_k \rho(x) \lambda_k u_k(x) u_k(y) / c_k\end{aligned}$$

$$= \rho(x) \sum_k u_k(x) u_k(y)$$

$$\therefore = 1$$

$$\hookrightarrow \lambda_k$$

$$\delta(x-y) = \rho(x) \sum_{k=1}^{\infty} u_k(x) u_k(y)$$

$$G(x,y) = \sum_{k=1}^{\infty} \frac{u_k(x) u_k(y)}{\lambda_k}$$

$$\mathcal{L} f(x) = h(x)$$

$$f(x) = \int G(x,y) h(y) dy$$

$$\mathcal{L} f(x) = \int \delta(x-y) h(y) dy$$

$$= h(x)$$

$$\partial_0 = \frac{\partial}{\partial x^0} = \frac{\partial}{\partial t}$$

$$\partial^0 = \frac{\partial}{\partial x_0} = -\frac{\partial}{\partial x^0} = -\frac{\partial}{\partial t}$$

$$\eta = (-1, 1, 1, 1)$$

$$\partial_1 = \frac{\partial}{\partial x^1} = \frac{\partial}{\partial x}$$

$$\partial^2 = \frac{\partial}{\partial x^2} = \frac{\partial}{\partial x^2} = \frac{\partial}{\partial y}$$

$$L = \frac{m}{2} \dot{q}^2 - V(q)$$

$$p = \frac{\partial L}{\partial \dot{q}} = m \dot{q}$$

$$\frac{\partial L}{\partial x^a} = 0$$

$$ds^2 = g_{ik} dx^i dx^k$$

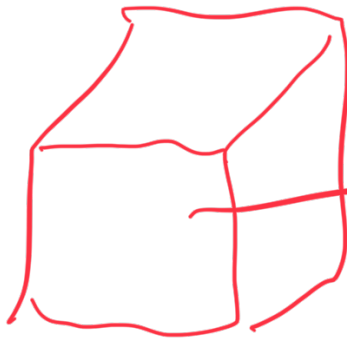
$$= \dots^2 + \dots + (dx^i)^2$$

$$= g_{00} dx^0 + g_{ik} dx^i$$

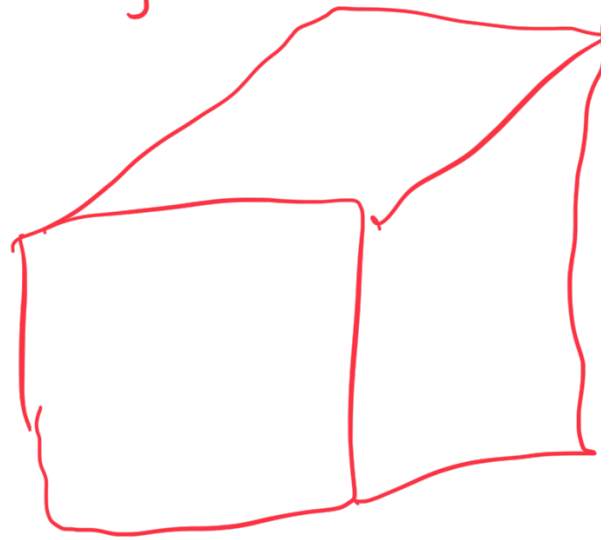
$$x^0 = ct$$

$$x^i \rightarrow r, \theta, \phi$$

$$g_{ik} \leftarrow g$$



less
energy



more
energy

$$p = - \frac{\partial u}{\partial V} < 0$$

$$\frac{\partial u}{\partial V} > 0$$

$$\sigma \propto V$$